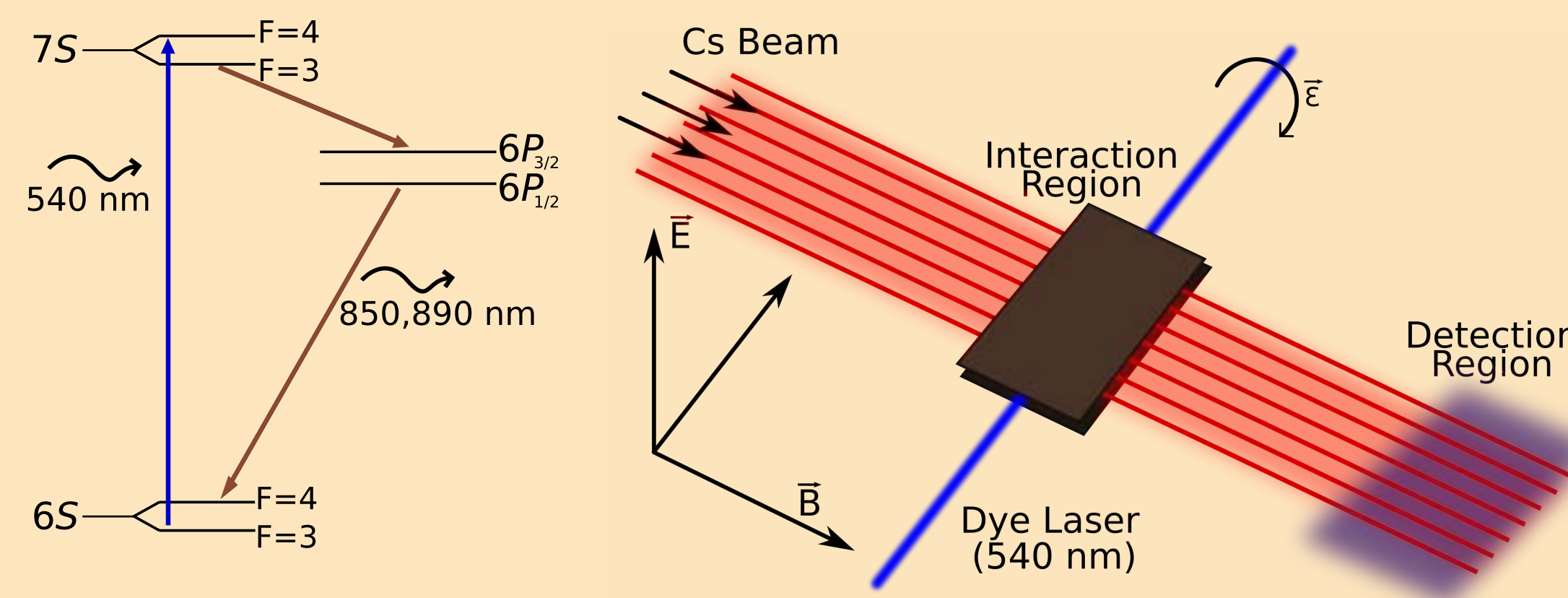


High-precision atomic structure theory: Electric dipole transition amplitudes

Benjamin M. Roberts, Carter J. Fairhall, Jacinda S. M. Ginges, arXiv:2211.11134

Electric dipole (E1) matrix elements

- Leading contribution to atomic transitions
- Determine lifetimes, decay widths
- Required for studies of
 - Atomic parity violation
 - Electric dipole moments
 - Atomic polarisabilities
 - Development of atomic clocks
 - Test atomic theory at the 0.1% level



Atomic Parity Violation

- Forbidden transitions become allowed: weak interaction
- Z-boson exchange between quarks and atomic electrons
- Measure rate: extract nuclear weak charge
- Weak charge: low-energy probe of Standard Model
- Atomic theory is bottle-neck. Strive for 0.1% accuracy

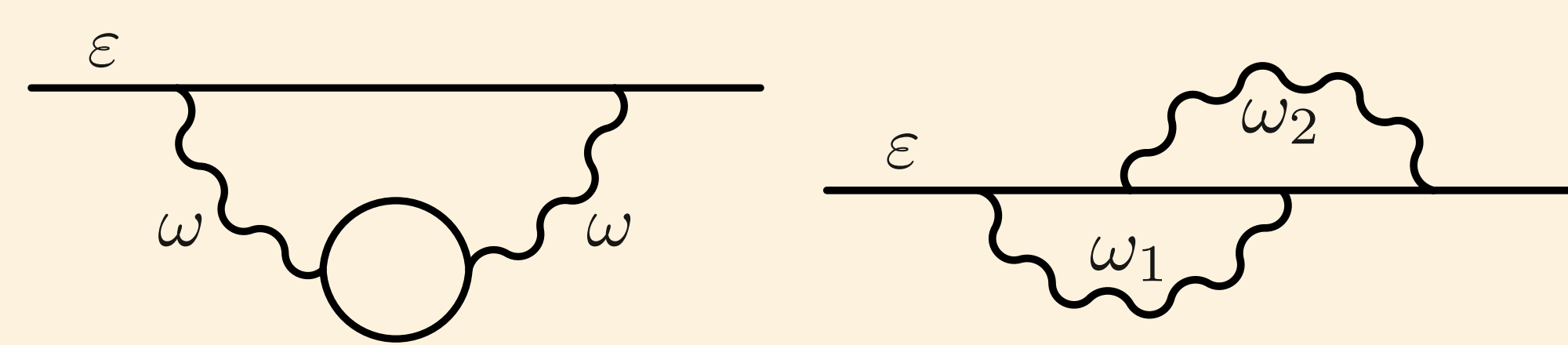
Wood, Bennett, Cho, Masterson, J. Roberts, Tanner, Wieman, Science 275, 1759 ('97)
 Theory: Dzuba, Flambaum, Ginges, Phys. Rev. D 66, 076013 ('02);
 Porsev, Beloy, Derevianko, Phys. Rev. Lett. 102, 181601 ('09);
 Dzuba, Berengut, Flambaum, BMR, Phys. Rev. Lett. 109, 203003 ('12)

Many-body atomic method: All-orders Feynman technique

- Accurate method based on Feynman diagram technique
- Dominating diagrams summed exactly to all-orders:
 - Screening of Coulomb interaction - polarisation of core
 - Hole-particle interaction (modification of HF potential)
 - Chaining of correlation potential (Brueckner orbitals)
- Core polarisation (RPA): all-orders in Coulomb interaction
- Highly accurate, highly stable, highly efficient
- No basis/spectrum required: integrate over frequencies
- Integration performed in complex plane: avoid poles
- Feynman Greens' function: evaluated at imaginary energies

Dzuba, Flambaum Sushkov, Phys. Lett. A 140, 493 (1989).

Correlation potential: direct and exchange

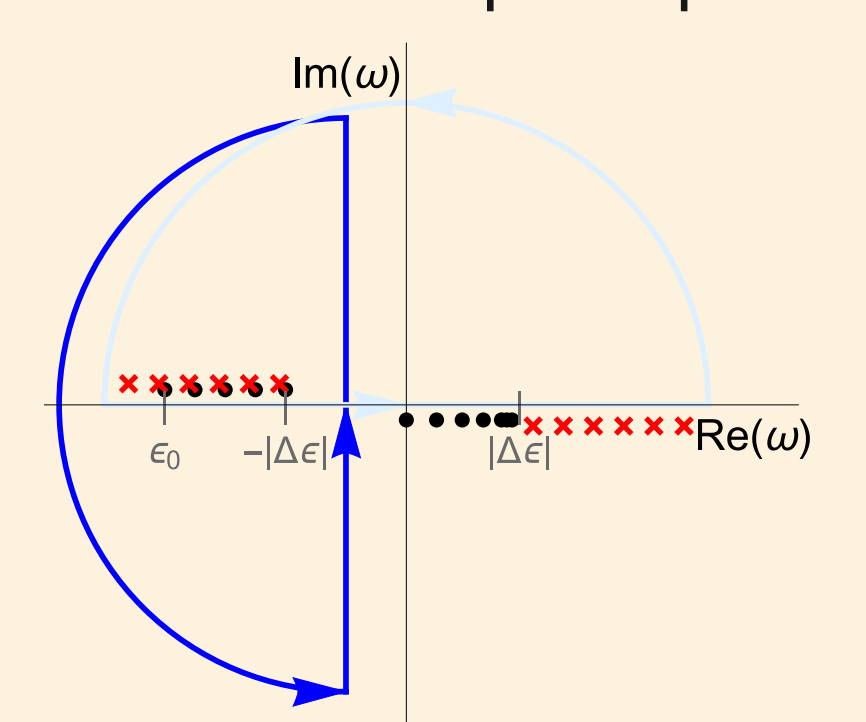


$$\Sigma(\text{direct}) = \int \frac{d\omega}{2\pi} G_{12}(\varepsilon + \omega) Q_{1i} \Pi_{ij}(\omega) Q_{j2}$$

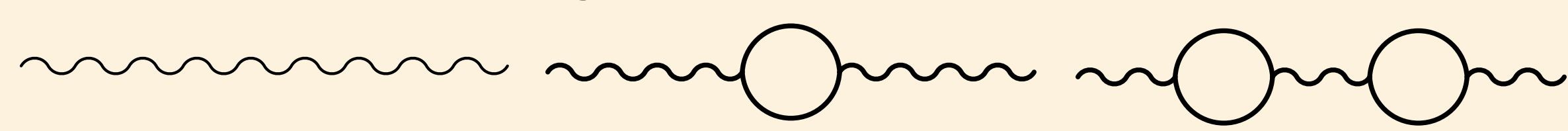
Polarisation operator:

$$\Pi_{12}(\omega) = \int \frac{d\varepsilon'}{2\pi} G_{12}(\varepsilon') G_{21}(\omega + \varepsilon')$$

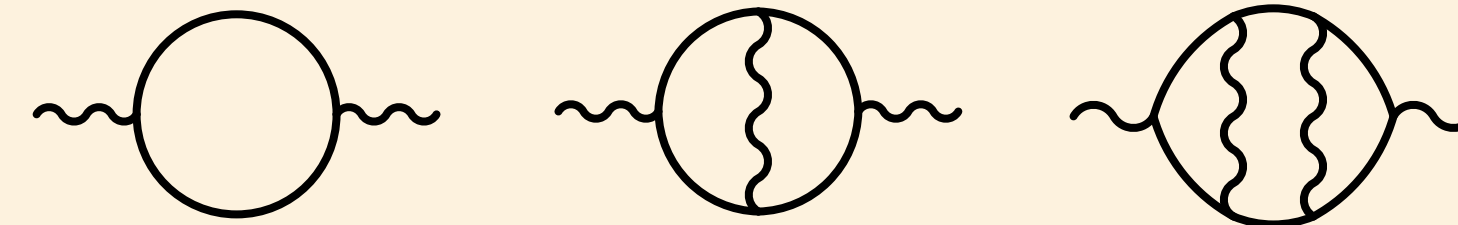
Rotate to complex plane:



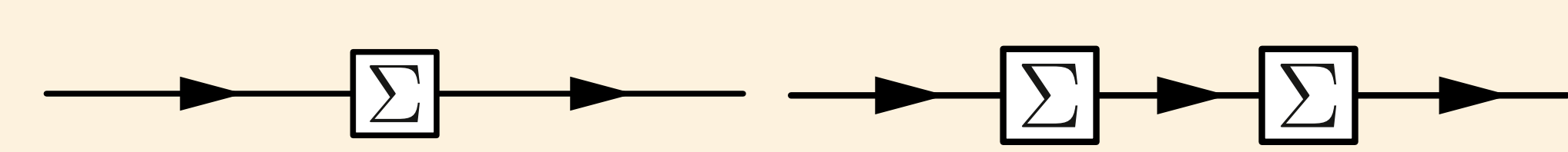
All-orders screening:



Hole-particle:



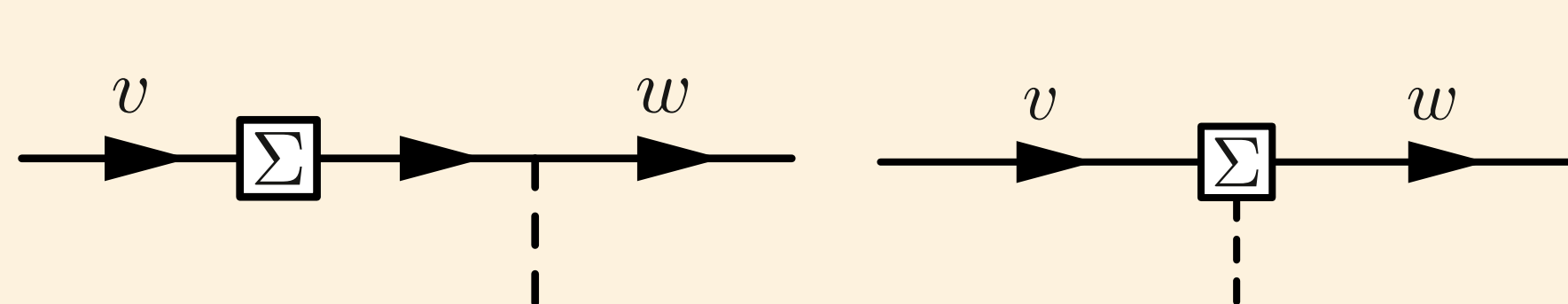
Chaining (Brueckner):



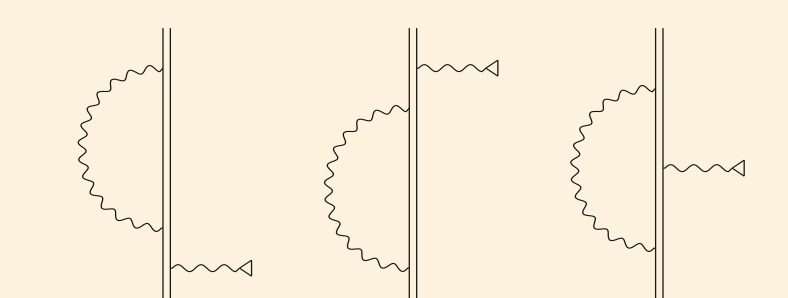
Other corrections:

- Structure radiation (external field inside correlations)
- Renormalisation of many-body wavefunction
 Johnson, Idrees, Sapirstein, Phys. Rev. A 35, 3218 ('87);
 Dzuba, Flambaum, Silvestrov, Sushkov, J. Phys. B 20, 1399 ('87)
- Breit (relativistic correction to Coulomb interaction)
 Derevianko, Phys. Rev. Lett. 85, 1618 (2000);
 Dzuba, Harabati, Johnson, Safronova, Phys. Rev. A 63, 044103 (2001)
- Radiative (one-loop) quantum electrodynamics
 Flambaum, Ginges, Phys. Rev. A 72, 052115 (2005)

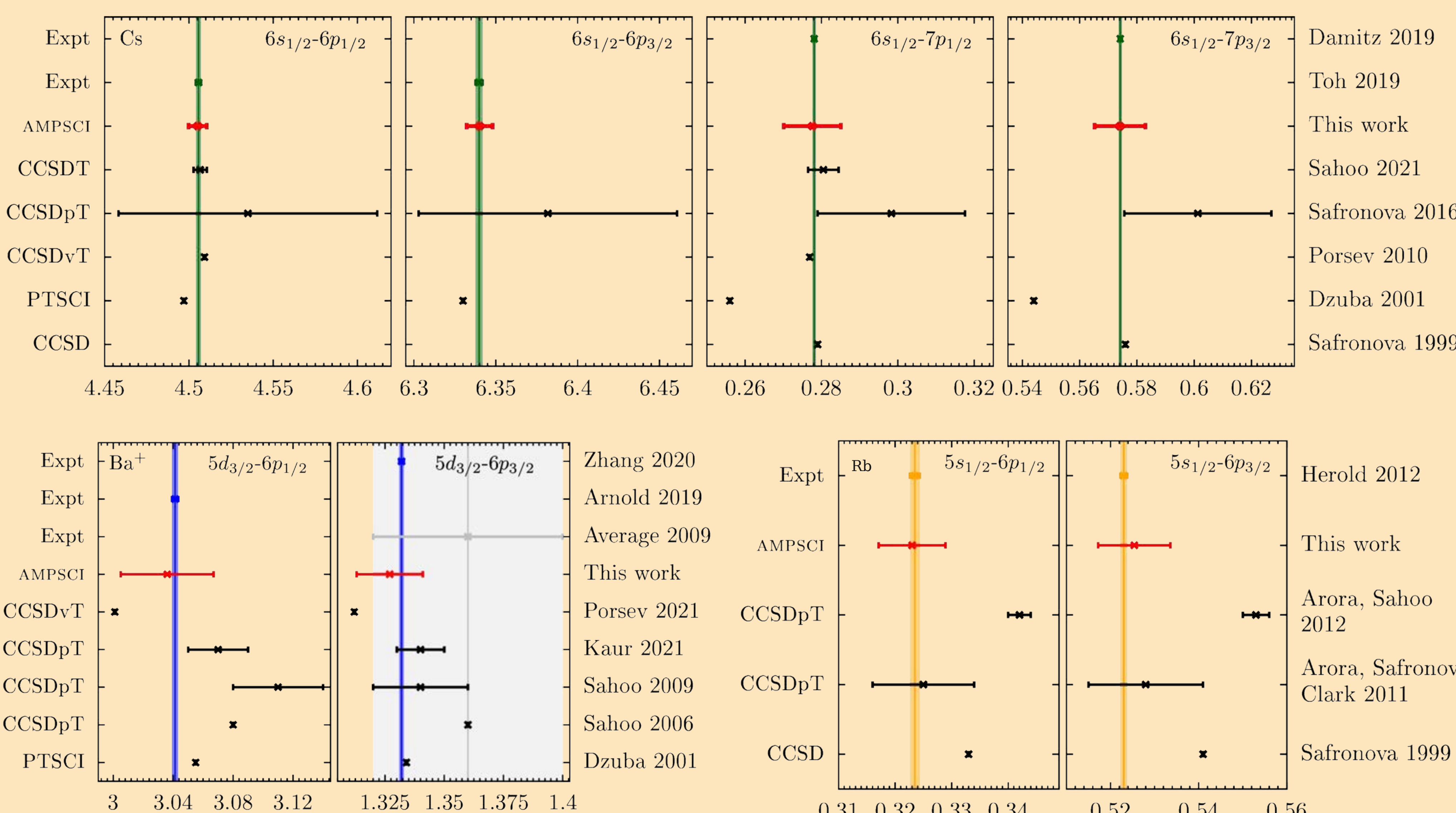
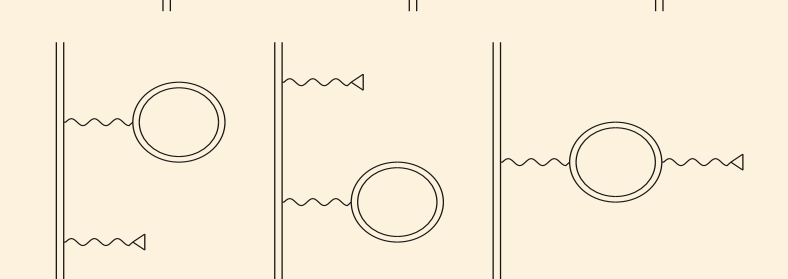
Structure Radiation:



Self-energy:



Vacuum Polarisation:



Results: Extraordinary Accuracy

- E1 amplitudes for s,p,d states of heavy atoms
- Alkali metals: K, Rb, Cs, Fr
- Alkali-like ions: Ca⁺, Sr⁺, Ba⁺, Ra⁺
- ~50 high-precision experimental E1 to compare
- + Large number of previous theory results
- Statistical analysis: better than expected
- Theory error-bars are robust, overly cautious
- 50% lie within experimental uncertainties: unprecedented theoretical precision
- Provably at level of 0.1% accuracy
- Some other calculations: underestimated errors

