

# Searching for dark matter with GPS and global networks of atomic clocks

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**NIST**

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Outline

Ultralight DM +  
TDs

Variation in clock  
frequencies

GPS

Initial search/  
first results

Bayesian search

Testing method

Possible  
outcomes

# Outline:

- Ultra light dark matter; “clumps”, e.g. Topological defects
- Transient signals: Global networks of precision devices
- GPS: 50,000km aperture sensor array
  - $\sim 30$  satellite clocks,  $> 15$  years of archived data
- Initial search: domain walls
- limits: orders of magnitude improvement for certain models
- Looking forward: Bayesian search technique

# Ultralight Dark Matter:

## WIMPs

- long-time “favourite” DM candidate
- Masses  $\sim 10 - 1000$  GeV
- Many null WIMP results
- Increased interest in other forms of DM

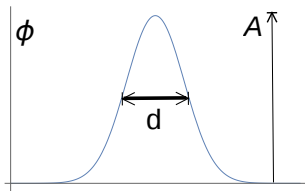
## Ultralight fields (e.g., axions)

- Masses  $\sim 10^{-24} - 1$  eV
  - Classical oscillating field:  $\phi = a \cos(m_a t)$
  - Stable topological defects: monopoles, strings, walls
    - Also: Q-balls, solitons, “clumps”
- 
- Peccei & Quinn '77, Weinberg '78, Dine & Fischler '82,...

# Topological Defect DM

## Topological Defects

- monopoles, strings, walls,
- Defect width:  $d \sim 1/m_\phi$
- Earth-scale object  $\sim 10^{-14}$  eV

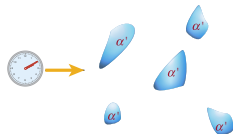


Inside:  $\phi^2 \rightarrow A^2$ ,

Outside:  $\phi^2 \rightarrow 0$

## Dark matter: Gas of defects

- DM: galactic speeds:  $v_g \sim 10^{-3}c$
- $A^2$ ,  $d$ ,  $\mathcal{T}_{b/w}$  collisions  $\implies \rho_{DM}$



$$A^2 = \rho_{DM} v_g d \mathcal{T},$$

- Sikivie '82, Preskil '83, Vilekin '85,  
Coleman '85, Lee '89, ...

# Possible DM–SM interactions

## Pseudoscalar (axionic) portal:

- e.g.,  $\mathcal{L}^{\text{PS}} = \partial_\mu a \bar{\psi} \gamma^\mu \gamma^5 \psi$
- Leads to magnetic-like interactions: magnetometry
  - GNOME: Global network of magnetometers (1)

## Quadratic scalar portal:

- Effective local shifts in values of fundamental constants
- Leads to shifts in clock frequencies
  - GPS.DM:  $\implies$  Global network of atomic clocks (2)

1. Pospelov, Pustelny, Ledbetter, Kimball, Gawlik, Budker, PRL **110**, 21803 (2013).
2. Derevianko, Pospelov, Nat. Phys. **10**, 933 (2014).

- Also: Interferometry etc.: Arvanitaki, Graham, Hogan, Rajendran, Van Tilburg (2016); Stadnik, Flambaum (2016)...

## Variation of fundamental constants

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$$-\mathcal{L}^{\text{S}^2} = \phi^2(r, t) \left( \frac{m_f \bar{\psi}_f \psi_f}{\Lambda_f^2} + \frac{1}{4\Lambda_\alpha^2} F_{\mu\nu}^2 + \dots \right),$$

c.f.  $\mathcal{L}^{\text{SM}} \implies$  transient additions to fundamental constants

$$\alpha^{\text{eff}}(r, t) = \alpha \left( 1 + \frac{\phi^2(r, t)}{\Lambda_\alpha^2} \right), \quad m_f^{\text{eff}}(r, t) = m_f \left( 1 + \frac{\phi^2(r, t)}{\Lambda_f^2} \right),$$

$\implies$  shifts in energy levels  $\implies$  shifts in clock frequencies

$$\frac{\delta\omega(r, t)}{\omega_0} = \phi^2(r, t) \sum_X \frac{K_X}{\Lambda_X} \quad K_\alpha : \text{Sensitivity of } \omega \text{ to } \delta\alpha$$

Flambaum, Tedesco, PRC, **73**, 55501 ('06); Flambaum, Dzuba, Can. J. Phys., **87**, 25 ('09).

# Shift in atomic clock frequencies

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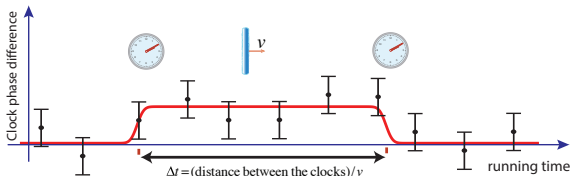
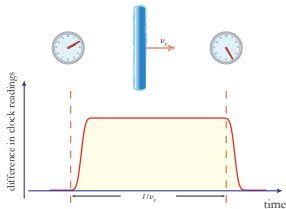
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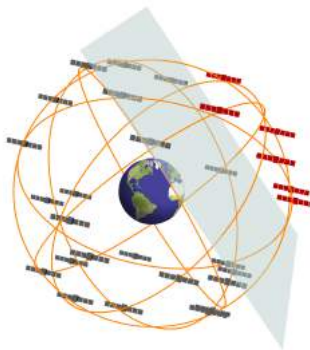
## Monitor Atomic Clocks

- Temporary frequency shift  $\rightarrow$  bias (phase) build-up
- Initially synchronised clocks become desynchronised



## GPS: 50,000 km DM observatory

- 32 satellite clocks (Rb/Cs),  $\sim 16$  years of high-quality data
- Also several H-maser ground-based clocks.
- Data from JPL: ([sideshow.jpl.nasa.gov/pub/jpligsac/](http://sideshow.jpl.nasa.gov/pub/jpligsac/))
  - 30s sampled data; 0.01–0.1 ns precision
- Correlated, directional signal, with  $v_g \sim 300$  km/s





## DM Walls: Initial search/limits

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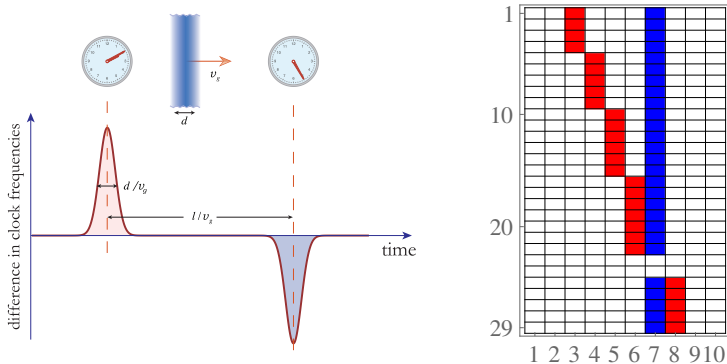
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- Thin wall: brief ( $< 30$  s) frequency excursion



- $\vec{v}$  encoded in time-delay and signal ordering:  $\Delta t \sim$  minutes

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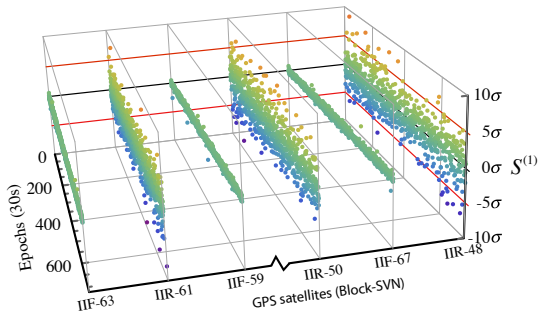
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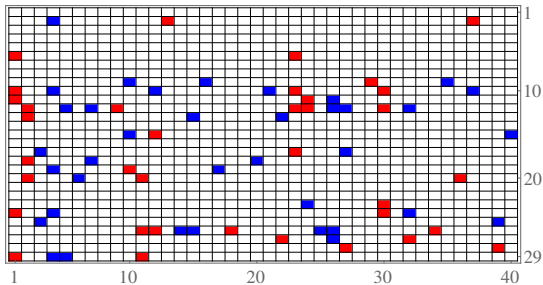
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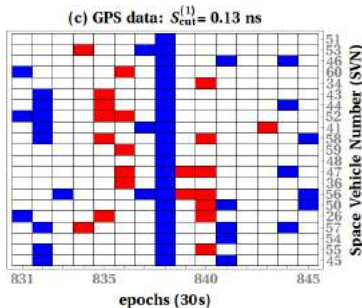
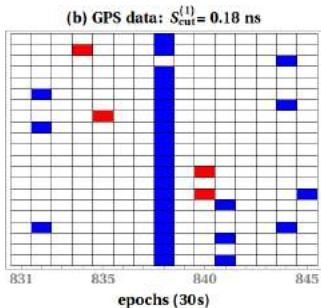
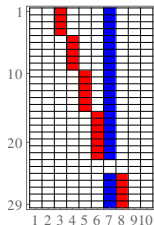
Apply  $S_{\text{cut}}$   $\implies$



## Scan the data

### Simple pattern search

- Match data windows against expected signals
- Reduce  $S_{\text{cut}}$  until signal can no longer be ruled out
- This case: excluded since  $\text{ref} > \text{rest}$



## Sensitivity

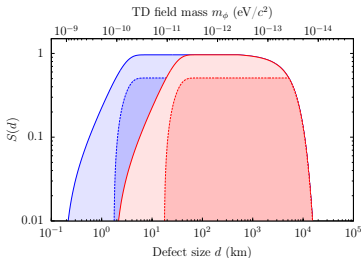
- 3D parameter space  $(\Lambda_X, \mathcal{T}, d)$ :

$$S = \hbar c \sqrt{\pi} \rho_{\text{DM}} \frac{K_X d^2 \mathcal{T}}{\Lambda_X^2}$$

$$\rho_{\text{inside}} = \frac{\rho_{\text{DM}} v_g}{d} \mathcal{T}$$

### Not equally sensitive to each width, $d$

- Assumes standard halo model
- “Servo time”:  $\tau = d/v_{\perp} > \tau_{\text{servo}} \approx 0.01 - 0.1 \text{ s}$
- Wall must be “thin” enough:  $\tau = d/v_{\perp} < 30 \text{ s}$



- Fraction of events we could “see”
- 90% C.L. (assuming SHM)

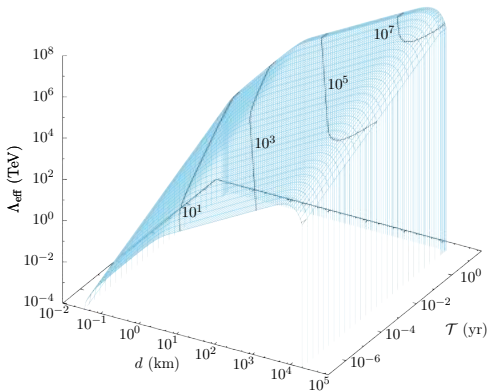
# Setting Limits

## What we see in the data:

- $S_{\text{lim}}^{(1)}$ : largest signal size that can't be ruled out
- Assume Poisson distribution, and SHM
  - $S_{\text{lim}}^{(1)} \sim 0.5 \text{ ns}$
  - $T_{\text{obs}} = 16 \text{ years}$

$$\frac{\Lambda_{\text{eff}}/\text{TeV}}{d/\text{km}} > 2 \times 10^3 \sqrt{\frac{T_{\text{obs}}s(d)/\text{yr}}{\lambda S_{\text{lim}}^{(1)}/\text{ns}}}.$$

## Results: Limits

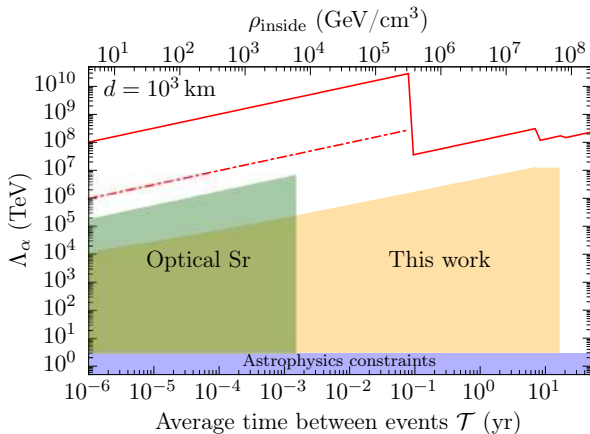


### Rb sub-network

- $\Lambda_{\text{eff}}$ : combination of  $\alpha$ ,  $m_{e,p}$ ,  $m_q$
- Until recently, existing limits did not exceed 10 TeV
- $\mathcal{T} = 1 \text{ yr} \ \& \ d = 10^3 \text{ km} \implies \rho_{\text{inside}} \approx 10^6 \text{ GeV/cm}^3$ 
  - c.f.  $\rho_{\text{water}} \sim 10^{24} \text{ GeV/cm}^3$

## Results: Limits - $\Lambda_\alpha$ (photon)

- (Assume this coupling dominates)



Sr: Wcislo, Morzynski, Bober, Cygan, Lisak, Ciurylo, Zawada, Nat. Astron. 1, 9 (2016).

Astro: Olive, Pospelov, Phys. Rev. D. 77, 43524 (2008).

# Results: Limits - fermion masses

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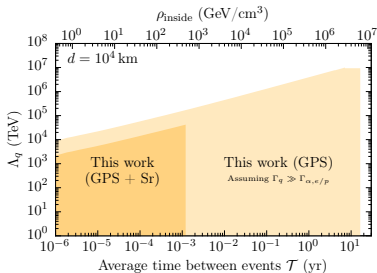
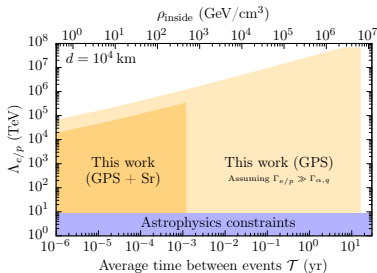
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## Combine Rb, Cs, and Sr (optical)

- Three different combo's of three couplings



Sr: Wcislo, Morzynski, Bober, Cygan, Lisak, Ciurylo, Zawada, Nat. Astron. 1, 9 (2016).

Astro: Olive, Pospelov, Phys. Rev. D. 77, 43524 (2008).



## How to improve upon this?

- There may be events “hiding” below the noise.
- Other geometries: monopoles, strings, thicker walls

### Bayesian Analysis

- Marginalise (integrate) all parameters (In-built Occam's Razor)
  - Time, velocity, object size, impact parameter
- Form odds ratios

$$\underbrace{p(D_{j_0} | m, I)}_{\text{Likelihood}} = K \underbrace{\int dx_1 \dots \int dx_n}_{\text{marginalise parameters}} \underbrace{p(x_1 \dots x_n | m, I)}_{\text{Priors}} \underbrace{\exp(-\chi_s)}_{\text{Gaussian likelihood}}$$

$$\chi_s = \sum_i^{\text{Clocks}} \sum_{jl}^{\text{Data}} (d_j^i - s_j^i) \widehat{H_{jl}^i} (d_j^i - s_j^i)$$

co-variance

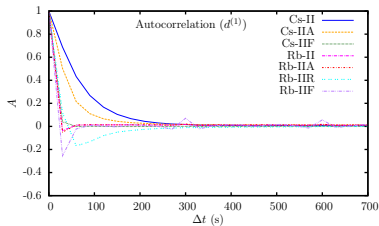
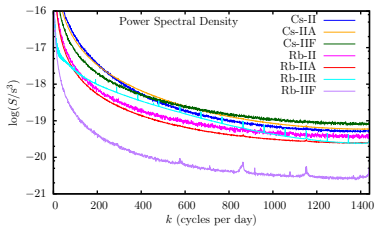
- Should be able to detect events as small as:

$$s \approx \sigma / \sqrt{N} \approx 0.001 \text{ ns (for the best clocks)}$$

## Test the method:

### Statistical properties of data:

- Power-spectrums, Auto-correlation functions, Allan variance, ...



- Generate “fake” data: mimics properties of the real data
  - $y$ : Input white noise,  $S$ : PSD,  $z$ : Simulated data

$$z = FT^{-1}(FT(y)\sqrt{S_{\text{target}}/S_y})$$

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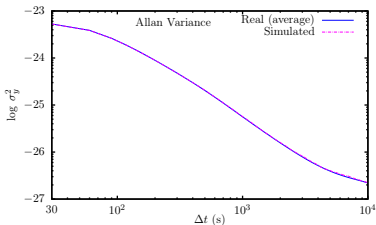
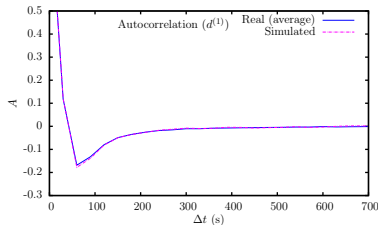
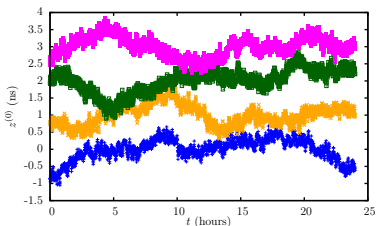
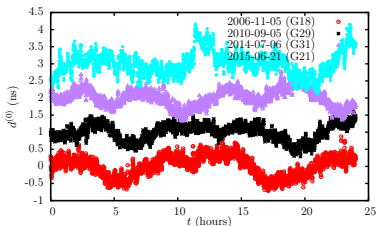
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## Test the method:



- Inject fake events: True positive rate
- Don't inject events: False positive rate
- Currently running large-scale simulations. Results promising!

## Possible outcomes:

### a) See ( $\sim$ few) very good candidate events

- Large odds ratio, good fit to model
- “best” case scenario: Analyse these in great detail
- Check against other precision experiments

### b) we don't

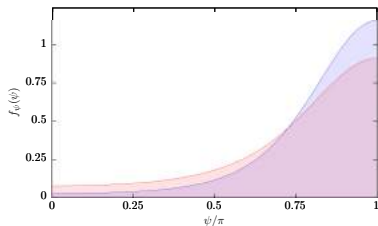
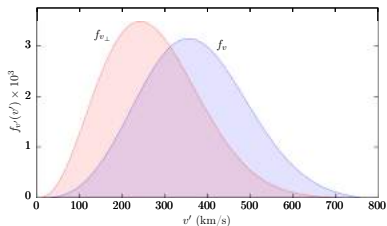
- Set limits.
- Is that all?
- Case when there is a large number of small events?

## Possible outcomes:

- All actual events should\* have same sign

## Vector velocity resolution:

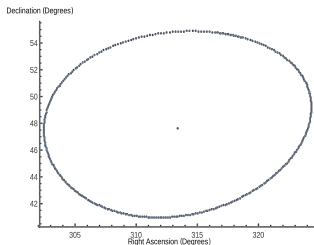
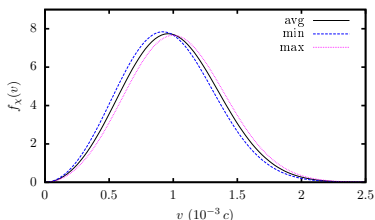
- $> 30$  clocks: quite good speed/direction resolution
- Potential to resolve velocity distribution (SHM)



- False positives will have different distribution
- But: have to “discount” priors for this analysis)

## Possible outcomes:

### Annual variation:



### Lower threshold. Lots of false-positives

- Assymetry in event 'sign' & resolve SHM predictions, +
- Annual modulation:
  - Event rate
  - Average velocity
  - Most-common incident direction

May extend discovery reach for  $\mathcal{T} \ll 1 \text{ yr}$  and  $d \ll R_{\text{GPS}}$

## Some references:

### Axions, ultralight scalar DM:

- R. D. Peccei and H. R. Quinn, Phys. Rev. Lett. 38, 1440 (1977).
- P. Sikivie, Phys. Rev. Lett. 51, 1415 (1983); Phys. Rev. Lett. 48, 1156 (1982).

### Topological defect DM:

- T. W. B. Kibble, Phys. Rep. 67, 183 (1980).
- A. Vilenkin, Phys. Rep. 121, 263 (1985).

### non-topological solitons, Q-balls:

- S. Coleman, Nucl. Phys. B 262, 263 (1985).
- K. Lee, J. A. Stein-Schabes, R. Watkins, and L. M. Widrow, Phys. Rev. D 39, 1665 (1989).
- A. Kusenko and P. J. Steinhardt, Phys. Rev. Lett. 87, 141301 (2001).

### Other non-gravitational TD searches:

- M. Pospelov, S. Pustelny, M. P. Ledbetter, D. F. J. Kimball, W. Gawlik, and D. Budker, Phys. Rev. Lett. 110, 21803 (2013).
- Y. V. Stadnik, V. V. Flambaum, Phys. Rev. Lett. 113, 151301 (2014); PRL 114, 161301 (2015).
- E. D. Hall, T. Callister, V. V. Frolov, H. Miller, M. Pospelov, and R. X. Adhikari, arXiv:1605.01103.
- P. Wcisło, Morzynski, Bober, Cygan, Lisak, Ciuryło, M. Zawada, Nat. Astron. 1, 9 (2016).

## Conclusion:

### GPS: 50,000km aperture DM observatory

- Topological defect dark matter/transient exotic physics
- GPS: 50,000km aperture sensor array
  - $\sim 30$  satellite clocks, many earth clocks,  $> 15$  years of clock data
- DM walls: Orders of magnitude improvement for certain models
- Looking forward: Bayesian search technique
  - Monopoles, strings, signals below  $\sigma_{\text{clock}}$
- General technique: archived, time-stamped data

More: see [arXiv:1704.06844](https://arxiv.org/abs/1704.06844), BMR<sup>1</sup>, G. Blewitt<sup>1</sup>, C. Dailey<sup>1</sup>, M. Pospelov<sup>2,3</sup>, A. Rollings<sup>1</sup>, J. Sherman<sup>4</sup>, W. Williams<sup>1</sup>, and A. Derevianko<sup>1</sup>.

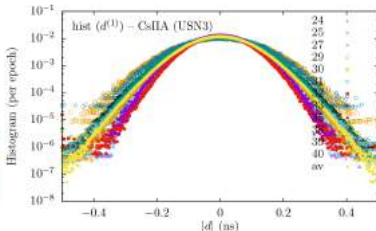
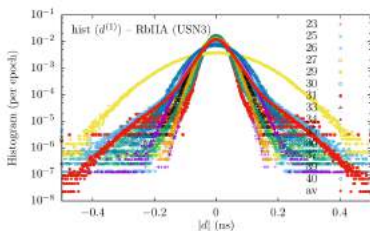
<sup>1</sup>University of Nevada, Reno; <sup>2</sup>Perimeter Institute; <sup>3</sup>University of Victoria, BC; <sup>4</sup>NIST Boulder





## Aside: challenges of re-purposed data

### data from JPL: Histogram



- Possible that some clocks mis-identified  
(Here, one of the “Rb” clocks is probably Cs).
- Same discrepancy in autocorrelation function, Allan variance etc.

# Clock stability: Mixed network

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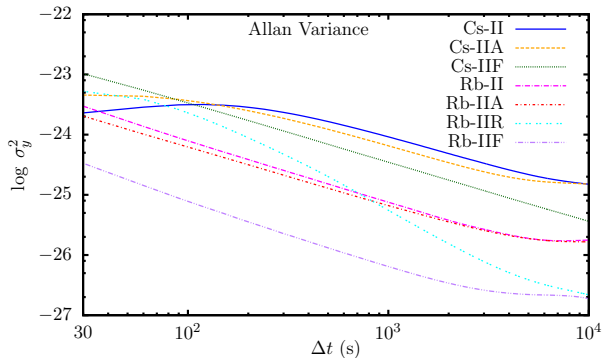
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## Launched:

- 1989–1997: II + IIA =  $\sim 17\,000$  clock-days
- 1997–2009: IIR =  $\sim 64\,000$  clock-days
- 2010–2016: IIF =  $\sim 8\,000$  clock-days
- Block III: Due in 2016 2017 2018(?)